

Reducing the Computation Complexity of 2-D Gaussian Filter

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Abstract—Now a day's we are facing a problem regarding smoothing of the image. One of the very useful method to smoothing the image is 2-D Gaussian Filter, which is used in Image Processing. However, the heavy computational resources are required by 2-D Gaussian Filter, and it comes down to real-time applications. The vital efficiency is achieved in this implementation. We use floating-point representation, but there are certain obstacle for this implementation because it requires large computational power in order to achieve real-time image processing. On the other hand a fixed-point approach is much more suitable for the implementation of a 2-D Gaussian filter in FPGA. By using fixed-point arithmetic for the implementation, the efficiency is increases, size of area decreases, complexity decreases and the computational cost is also reduced. In this paper we reduced the LUT by 11.34 % by using Gaussian filter.

Keywords—LUT-Look up table, real-time Gaussian filter, fixed-point, computational cost

1. INTRODUCTION

We are living in digital words. Digital world means technical and modern world. The idea of digital image processing are being applied in different fields such as medicine, astronomy, geography, industry, etc. [1]. These fields often require results in real-time, and efficiency in the implementation of digital image processing is imperative. In this paper, we present how the LUT is reduced by the implementation of a 2D Gaussian Filter on an FPGA [2].

Image Processing is processing of images using mathematical operations by using any form of processing for which the input is an image, a series of images, or a video. Image processing are basically a digital processing but optical and analog image are also possible [3]. Computer graphics and computer vision are also related to image processing. Images are manually made from physical models of objects, environments, and lighting, instead of being acquired (via imaging devices such as cameras) from natural scenes, as in

most animated movies [4]. On the other hand computer vision is often considered high-level image processing out of which a machine/computer/software intends to decipher the physical contents of an image or a sequence of images (e.g., videos or 3D full-body magnetic resonance scans) [5]. In this paper we take an example of convolution using FPGA was developed using [3*3] sobel filter using a [15*15] image. [6].

The remaining paper is divided into 4 sections. Section 2 covers the theory, Section 3 explains the methodology of the Gaussian filter; shows a performance of the Gaussian filter and Kernel Quantization; while Section 4 presents the hardware implementation for the Gaussian filter for fixed-point. In Section 5, the results of the filter implementations are discussed and give the conclusion.

2. THEORY

I. Role of Filters

For increasing the sharpness and brightness of the image we use a filter circuit. To emphasize a desired feature or to remove an undesired feature we use a filter. Any image can be represented by a matrix of pixels with values ranging from 0 to 255 [7]. For an example we send a [512 x 512] image to the FPGA requires converting that image into a vector of 261244 elements, where DATA is the pixel value and ADDR is the memory address of each pixel [8].

II. Image Smoothing

Smoothing is the process which is used to control the extent of smoothing because it is a tuning parameter. The main purpose of smoothing is to remove the noise or other unwanted phenomena. In smoothing the images are modified so that the individual points are noise free. There are two important causes in which smoothing is used that can aid in data analysis [9].

III. Sharpening Filters

Image sharpening means to emphasize the shape and drawing the viewer's focus. If the high frequencies are attenuated or completely removed, then the visual quality of an image will be poor. In other words we can say that if the high frequency components of an image are used then the quality of the image is improved. Image sharpening means to enhance the highlighted edges and fine details in an image. For an effective sharpening process we generally use the high-pass filter operation. Basically a linear filter has been used in the implementation of a high-pass filter [10].

3. METHODOLOGY

I. Gaussian filter

For a smooth and noise-free image, the Gaussian filter is used, which is a 2-D convolution operator. The convolution of an image $w(x,y)$ of size $m \times n$ with a function of $f(x,y)$ [10], denoted by $w(x,y) \cdot f(x,y)$, is

$$w(x,y) * f(x,y) = \sum_{s=-a}^a \sum_{t=-b}^b w(s,t) f(x-s, y-t)$$

given by equation (1),

In this equation a and b are given by $a = (m-1)/2$ and $b = (n-1)/2$. Figure 1 illustrates the graphical representation of equation (1). Function $f(x,y)$ defines the Gaussian filter, established by the

$$f(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}} \quad (2)$$

Gaussian distribution in equation (2):

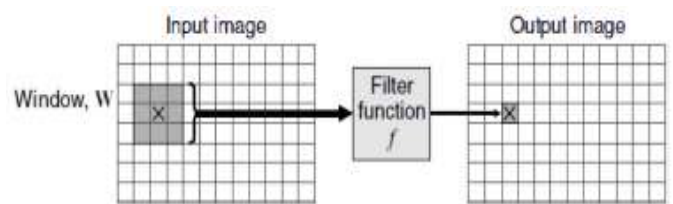


Figure 1. A window filter. The shaded pixels represent the input window that produced the filtered value for the corresponding location in the output image. Each possible window position generates a corresponding location in the output image [8].

The dimensions of the windows and the standard deviation are the two parameters of the Gaussian filter. We required a large standard deviation for the smoothing image.

This filter also reduced some noise like "salt and pepper" and extracting features on the SALT algorithm [11], salt and pepper noise are shown in figure (2).

Figure 2. Image with 30% salt & pepper noise

For the perspective of spatial and frequency domains, Gaussian smoothing filters are low-pass filters. These filters are efficient to implement and can be generally used by engineers in practical vision applications [6].

II. 2-D Gaussian Filter

There are various Gaussian function like 1D, 2D and ND, whose expression are as follows:

$$G_{1D}(x) = \frac{1}{\sqrt{2\Pi}\sigma} e^{-\frac{x^2}{2\sigma^2}} \tag{3}$$

$$G_{2D}(x, y) = \frac{1}{\sqrt{2\Pi}\sigma} e^{-\frac{x^2+y^2}{2\sigma^2}} \tag{4}$$

$$G_{ND}(\vec{x}) = \frac{1}{\sqrt{2\Pi}\sigma} e^{-\frac{|\vec{x}|^2}{2\sigma^2}} \tag{5}$$

Where width of the Gaussian functions is indicated by σ . If we considered the Gaussian probability density function, then σ is considered as a standard deviation and variance (σ^2) is the square of standard deviation [12].

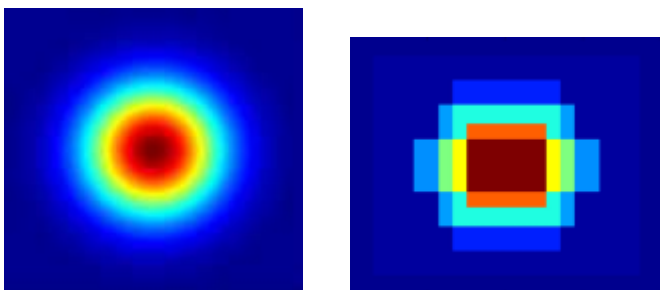
The 2-D Gaussian function in discrete version is shown in equation (6)

$$G_n(x, y) = K_n \times e^{-\frac{(x^2+y^2)}{2\sigma^2}} \tag{6}$$

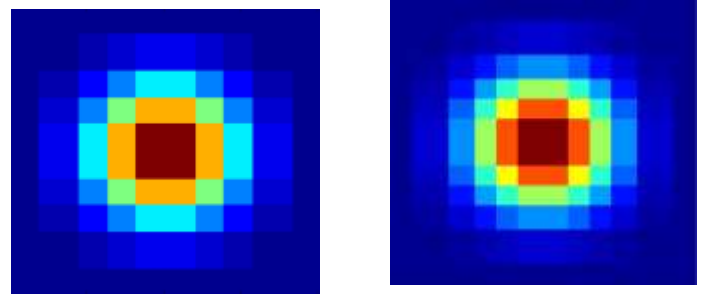
where spatial coordinates are indicated by x and y, where M * N represents the kernel size, n is preferred as 1,2 and 3, if the Gaussian function is designed with three scales, namely, 16, 64, and 128.

III. Kernel Quantization

Gaussian filter is implemented in FPGA by using VHDL description language. In this filter the addition and multiplication are process in between the image and the kernel, where image is represented by a matrix with value 0 to 255 98 bits). The normalized square matrix is kernel, which values are between 0 and 1.



(a)Gaussian kernel (b) SII [24] approximation



(c) Proposed approximation (4 constant) (d) Proposed approximation (5 constant)

Figure 3. Comparison of (a) exact Gaussian kernel, (b) stacked integral images [13] with 5 2-D boxes, and the proposed method with 4 constants (c) and 5 constants (d). [14]

4. HARDWARE IMPLEMENTATION

Any image can be represented by a matrix of pixels with values ranging from 0 to 255. Sending a [512 x 512] image to the FPGA requires converting that image into a vector of 261244 elements as shown in Figure 4, where DATA is the pixel value and ADDR is the memory address of each pixel, respectively.

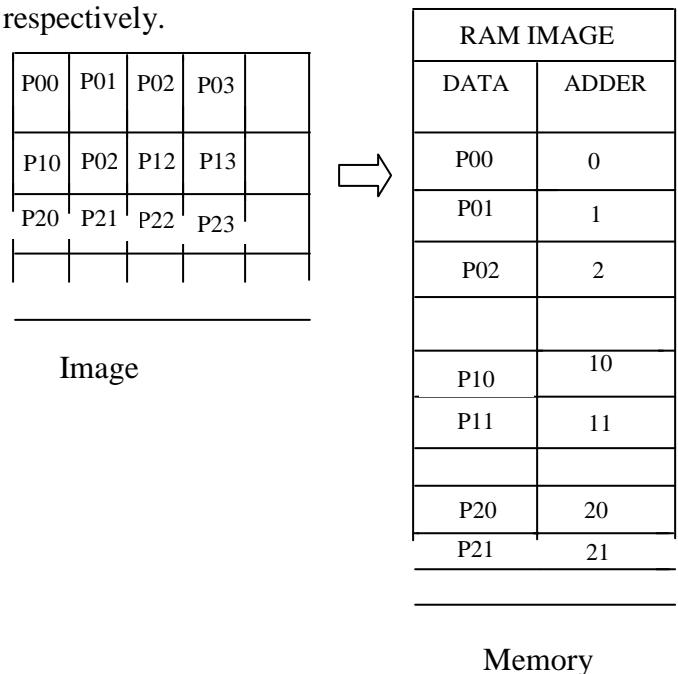


Figure 4. Conversion of an image Matrix to an image vector

Each [3*3] sun image is extracting from the original image, from top to bottom, and from left to right, occurs in the convolution of an image with a [3*3] kernel. After that kernel image are multiplied with

each element, and the resulting products are finally added together (by using multiply-accumulate – MAC- operation), and finally returned to an output pixel. MAC process is explained in figure (6).

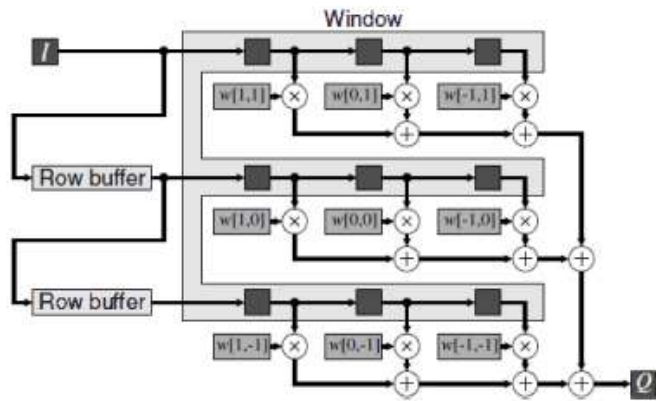


Figure 5. Extraction of a [3*3] sub image and MAC operation [8]

In Figure 5, the row buffer is used to store the rows of pixels belonging to the [3*3] window neighborhood. Shift registers are used to store the pixels from these rows. We required N-1 rows buffers to solve the convolution of N*N. FIR Filtering is same as this process.



Figure 6. Fixed point representation

5. RESULT

The usage of FPGA resources using fixed point method for a [3*3] kernel and a standard deviation 0.5 is taken. As the kernel size increases, the use of LUTs and slice registers will be increases by internal implementations of FIFO memories. In our design we see that the implementation of a 2-D Gaussian filter in FPGA.

Table 1: Comparison between with and without Gaussian filter

Resource	Estimation without Gaussian filter	Estimation with Gaussian filter
FF	76	106400
LUT	86	53200
I/O	1	200

By using fixed-point arithmetic for this implementation, the efficiency is increases, size of area decreases, complexity decreases and the computational cost is also reduced. In this paper we reduced the LUT by 11.34 % by using Gaussian filter, we can see in Table 1.

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